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XLV. A second Letter to the Right Hon.
the Earl of Macclessield, President of the
Royal Society, concerning the Transit of
Venus over the Sun, on the 6th of June
1761; by the Rev. Nathanael Bliss, M. A.
Savilian Professor of Geometry in the University of Oxford, and F. R. S.

My Lord,

Read Jan 7, HE interior conjunctions of the planets Mercury and Venus, that happen near the ecliptic limits, have always engaged the attention of astronomers, as they furnish the best means of determining some of the most important elements in the theory of those Planets. The transits of the former have been often and carefully observed by the most eminent astronomers, ever fince the invention of the telescope; and, it may be presumed, that the elements of Mercury's theory are established as accurately as can be expected. The opportunities of observing Venus upon the sun's disk occur so seldom, that the astronomers of these days have reason to think themselves peculiarly happy, in being eye-witnesses of so rare a phænomenon; more particularly too, as the advantages resulting from the observations of this transit, are, in all probability, of the greatest moment. The first, and only observation of this kind, was made by our ingenious countryman, the Rev. Mr. Jeremiah Horrox, a young gentleman of very distinguished abilities, who, by his own observations, with instru-

ments constructed under his own inspection, and finished by his own hands, was enabled to correct the so much boasted tables of Lansbergius, and to predict, with a degree of precision unknown to those times, a phænomenon, which he himself thought to be of great consequence. He immediately communicated this important discovery to his friend, and companion in his aftronomical studies, Mr. William Crabtree, and earnestly exhorted him to prepare for the observation. The state of the heavens, on that day, was not very favourable: however, both Mr. Horrox and his friend were lucky enough to observe it; the former, at a time when the limbs of the fun and Venus were in the point of contact, viz. on the 24th of November 1639, O.S. And these two were the first, and only persons, that ever saw Venus in the fun, before the present year.

By the Rudolphine tables, constructed from the observations of Tycho Brahe, Kepler was enabled to predict, in the year 1629, that Venus would pass over the sun's disk in the year 1761: and my worthy predecessor, that eminent astronomer and mathematician, Dr. Halley, in a memoir published in the Philosophical Transactions, No 348. exhorted the astronomers of all countries to attend to this rare phænomenon, with all possible diligence; as it would furnish them with the best means of determining the parallax and distance of the sun, and, consequently, the dimensions of the whole solar system. How far the method proposed by him, will enable us to solve this difficult problem, must be left to time to discover, when the observations, made in places properly situated, can be compared with those made here, and Vol. LII. Ηh in

in other famous observatories. The attention paid to the opinion of an English astronomer, by the most renowned Princes, more particularly by his late Majesty, at the request of your Lordship, and the Royal Society, will reflect the greatest honour upon their names, to the latest posterity. But as the tables, which Dr. Halley made use of, were very imperfect, his own not being then constructed, and did not represent the place of Venus on the sun with that accuracy, which the method, in this case, required: and as that eminent philosopher committed a small mistake in his calculations, by placing the axis of Venus's path, and the axis of the equator, on the same fide of the axis of the ecliptic; a mistake which the most accurate calculator might easily fall into: from these considerations, I say, the honour of determining the fun's true parallax is, probably, referved for the reign of his present Majesty; from whom, as a patron of science, and every useful art, we have the greatest reason to promise ourselves every possible encouragement and affiftance.

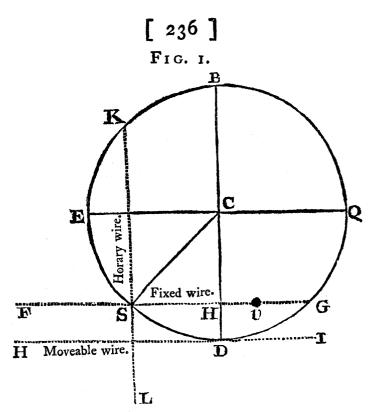
I have already had the honour of presenting to your Lordship, and the Royal Society, an account of the observations of the contacts of the sun's and Venus's limbs, made at Greenwich, and at your Lordship's own observatory. As the time would not then permit me to examine the observations made with the micrometer, I could only select a few particulars, relating to the diameters of the sun and Venus, as measured by different observers. I have since had leisure to examine all the observations made upon the day of the transit, both at Shirburn castle, and at the Royal Observatory at Greenwich; and shall now beg

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leave to lay before you, both the observations themfelves, and the several results deducible from them

by calculation.

The method of determining the right ascension and declination of the center of Venus from that of the fun, was the fame which Dr. Bradley used, in observing a former transit of Mercury. The planet was made to run down the fixed wire of the micrometer, and the difference of the time of passage was observed between it, and that part of the sun's limb, which was cut by that wire; and the moveable wire was brought to touch the sun's lower limb. If the fun's lower limb had been made to run down the fixed wire, and the moveable wire brought to the planet, and the difference of the time of passage had been observed between it and the sun's confequent limb, on the supposition, that the wire was not exactly parallel to the diurnal motion, it would have caused a considerable error in the difference of right ascension, observed at the distance of the sun's semidiameter. But the method we made use of requires fome calculation, to determine the position of Venus on the fun's disk.



Let, therefore, in Fig. 1. the circle EDQB represent the sun's disk, in which let EQ be parallel to the equator, and BD an hour-circle; let the pricked line FG represent the fixed wire of the micrometer, HI the moveable wire, and KL the perpendicular or horary wire. The difference of right ascension Hv, and of declination CH, will be determined in the following manner: SC, or CD, the semidiameter of the sun is given, and CD — DH — CH, the difference of declination; and SC and CH being given, SH may be found; and then the observed difference of right ascension Sv being diminished

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minished in the ratio of radius to the fine of the polar distance of Venus, will give HU, the difference of

right ascension.

As the clouds began to disperse, and the sky to become favourable, at Shirburn castle, above two hours before we had any opportunity of observing at Greenwich, I shall first give the observations there made by Mr. Hornsby, and afterwards my own at Greenwich. But here I would be gleave to premise, that, though the numbers are given to parts of a second, the observers do not pretend to an imaginary exactness, (for they did not estimate the times of passage nearer than a quarter of a second of time) but the numbers are such as result from the turning minutes and seconds of time into motion, and the revolutions and parts of the screw of the micrometer into minutes and seconds.

The fun's horizontal diameter, as measured by the micrometer, was 31' 33", and that of Venus, by several observers, 58"; the following observations were therefore deduced, by assuming the semidiameter of the sun = 15' 46". 5, and that of Venus = 29'.

the fun = 15' 46".5, and that of Venus = 29'.

1. At 17^h 33' 50", apparent time, at Shirburn, the center of Venus preceded the part of the fun's limb, cut by the fixed wire, 12' $3\frac{2}{\pi}$ " in motion; and the north, or upper limb of Venus, was north of the fouthern, or lower limb of the fun, 6' 29".6: therefore, the center of the fun preceded the center of Venus in right ascension 1' 36".9; and the center of Venus was south of that of the sun in declination 9' 45".8. The same, to avoid repetition, in all the following observations.

2. At 17^h 35' 41", the center of Venus preceded the fun's limb 12' 13"; and the upper limb of Venus was north of the fun's lower limb 6' 19".7: fun's center, therefore, before that of Venus in right ascenfion, 1' 21"; and the center of Venus was south of the fun's center in declination 9' 55.7".

3. At 17^h 40' 1", Venus before fun's limb 12' $37\frac{1}{2}$ ", and was north of fun's lower limb 6' 18.2": therefore, fun's center, before that of Venus in right afcension, 57''.2; and Venus south of sun's center in

declination 9' 57".3.

N. B. In these observations, the sun's limb undulated.

4. At 17^h 43′ 59″, Venus before sun's limb 12′ 47″; and was north of sun's lower limb 6′ 16″.3: therefore, sun's center before Venus in right ascension 47″; and Venus south of sun's center in declination 9′ 59″.2.

5. At 17^h 50' 31'', Venus before sun's limb $13' 9\frac{1}{4}''$; and was north of sun's lower limb 6' 10''.4: therefore, sun's center before Venus in right ascension 22''; and Venus south of sun's center in de-

clination 10' 5".1.

6. At 18h 3' 41", Venus before fun's limb 13' 48½"; and was north of fun's lower limb 5' 59".2: therefore, the center of Venus was before the fun's center in right ascension 23".2; and was south of

fun's center in declination 10' 16".3.

7. At 18h 8' 54", Venus before fun's limb 14' 13"; and was north of fun's lower limb 5' 53".8: therefore, Venus before fun's center in right ascention 49".9; and was south of fun's center in declination 10' 21".7.

8. At

8. At 18^h 15′ 50″, Venus before sun's limb 14′ 33″; and was north of sun's lower limb 5′ 48″: therefore, Venus before sun's center in right ascention 1′ 13″.2; and was south of sun's center 10′ 27″.5 in declination.

9. At 18h 28' 6", Jenus before sun's limb 15' $9\frac{1}{4}$ "; and was north of sun's lower limb 5' 35".4: therefore, Venus before sun's center in right ascension 1' 57".2; and was south of sun's center in declination 10' 40".1.

10. At 19^h 18' 49'', Venus before sun's limb 18' $5\frac{1}{2}$ ''; and was north of sun's lower limb 4' 45''.5: therefore, Venus before sun's center in right ascention 5' 25''.3; and was south of sun's center 11' 30''.

11. At 19^h 22' 37", Venus before fun's limb 18' 9½"; and was north of fun's lower limb 4' 44".3: therefore, Venus before fun's center in right ascension 5' 29".9; and was south of sun's center 11' 31".2.

12. At 19^h 25′ 50″, Venus before fun's limb 18′ 23³″; and was north of fun's lower limb 4′ 42″.5: therefore, Venus before fun's center in right ascention 5′ 45″; and was fouth of fun's center 11′ 32″.9.

13. At 19h 29' 20", Venus before sun's limb 18' 31\frac{3}{4}"; and was north of sun's lower limb 4' 35".2: therefore, Venus before sun's center in right ascension 5' 59".8; and was south of sun's center in declination 11' 40".3.

14. At 19h 45' 58", Venus before sun's limb 19' 20½"; and was north of sun's lower limb 4' 19": therefore, Venus before sun's center in right ascension 7' 1".5; and was south of sun's center 11' 56".5.

15. At 19h 49', Venus before fun's limb 19' 28"; and was north of fun's lower limb 4' 16".6: therefore.

fore, Venus before sun's center in right ascension 7' 11".1; and was south of sun's center 11' 58".9.

16. At 20^h 12' 1', the center of Venus followed the sun's preceding limb, cut by the fixed wire, 1' 58"; and was north of sun's lower limb 3' 54".2: therefore, Venus before sun's center in right ascension 8' 34".2; and was south of sun's center in declination 12' 21".3.

The following observations were made by myself, at Greenwich, as soon as the sky became favourable.

1. At 19^h 38′ 21″, apparent time, at Greenwich, the antecedent, or first limb of Venus, preceded that part of the sun's limb cut by the fixed wire 18′ 48½″ in motion; and the center of Venus was north of the southern, or lower limb of the sun, 4′ 4″.5: therefore, the center of Venus preceded the sun's center in right ascension 6′ 18″.9; and was south of that of the sun in declination 11′ 42″.1.

2. At 19^h 42' 9'', the limb of Venus before fun's limb 18' $52\frac{1}{2}''$; and was north of fun's lower limb 3' 56''.8: therefore, Venus before fun's center in right ascension 6' 31''; and was south of it in declination 11' 49''.7. But this is marked as dubious.

3. At 19h 44' 35", limb of Venus before fun's limb 19'; and center was north of fun's lower limb 3' 57".5: therefore, Venus before fun's center in right ascension 6' 37".1; and was south of fun's center in declination 11' 49".

4. At 19^h 53' 14", limb of Venus before fun's limb 19' 22½"; and was north of fun's lower limb 3' 51".3: therefore, Venus before fun's center in right ascention 7' 5"; and was south of sun's center in declination 11' 55".2.

5. At

5. At 19^h 58' 26", limb of Venus before sun's limb 19' $37\frac{1}{2}$ "; and was south of sun's lower limb 3' 43": therefore, Venus before sun's center in right ascension 7' 28".6; and was south of sun's center in declination 12' 3".5.

The few observations, which were afterwards made by Mr. Green, with Mr. Dollond's micrometer, are omitted; for they disagree so much with themselves, and also with the above, that there must be some error in reading the numbers of the nonius; or, which is more probable, in placing the micrometer exactly parallel to the equator, occasioned by the hurry

with which they were made.

In order to determine more exactly the time of the ecliptic conjunction, with the latitude of Venus then; together with the time of the middle of the transit, and the nearest approach of the centers; and from thence the true place of her node; I have carefully computed the following numbers from theory: because, as Dr. Halley has observed, in the Philosophical Transactions, No 386, "there is always an unavoidable, though imall uncertainty in what we observe, yet greater than there can be in the theory, espe-" cially now it is so very near the truth." The solar numbers were computed from new tables, not yet published, corrected by the small equations, occafioned by the influence of the moon and planet Jupiter, and also the nutation of the earth's axis. fun's place was very well observed on the meridian, both at Greenwich and Shirburn, the day of the transit; which, allowing for the difference of longitude of those places, agreed to a surprizing exactness, within two seconds; and did not differ more than five

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feconds in excess from the computed place. The place of Venus was computed from Dr. Halley's tables, only adding 31" to the mean motion, and 1' 45" to the place of the node; by which corrections, they had been found to agree better with observations made near the inferior conjunction in

1753

According to these numbers, the ecliptic coniunction of the sun and Venus was June 5, 1761, N. S. at 17h 51' 20", mean time, at Greenwich: and the place of the fun and Venus 2f 15° 36' 33"; and the geocentric latitude of Venus fouth of 44".g. The places of the fun and Venus being computed for three hours before, and three hours after the ecliptic conjunction, the horary motion of the fun is 2' 23".45; of Venus retrograde 1' 33".68: the horary motion of Venus from the fun, therefore, 3' 57".13, retrograde. The horary motion of Venus in latitude is south 35".46. The angle of the visible way with the ecliptic 8° 30' 10"; the horary motion in that way 3' 59".77. The right ascension of the sun, supposing the apparent obliquity of the coliptic 23° 28' 18", was then 74° 22' 19".2; and the horary motion of the fun in right ascension was 2' 34".55. The declination of the fun was then 22° 41′ 35".9; the horary motion in declination was 15".33 northwards. The angle formed by the axis of the ecliptic, and the axis of the equator, was 6° 9' 34", decreasing hourly one minute.

The right ascension of Venus, at the ecliptic conjunction, was 74° 23′ 27″.2; and the horary motion of Venus in right ascension 1′ 36″.75 retrograde. The horary motion of Venus from the sun in right

ascension,

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ascension was, therefore, 4' 11".3 retrograde. The declination of Venus was then 22° 31' 54".2; and the horary motion in declination was 45".29, southwards: the horary motion of Venus from the sun in declination was, therefore, 1' 0".62, southwards.

The logarithm of the earth from the sun was then 5.006642; the logarithm of Venus from the sun was 4.861192; and the logarithm of Venus from the earth was 4.460874. If we suppose the horizontal parallax of the sun to be 10½, then the horizontal parallax of Venus, as seen from the earth, will be 36″.31; which, diminished by that of the sun, is 25″.97. If the parallax in longitude and latitude is computed from these data, the visible horary motion of Venus from the sun in longitude will be 3′ 58″.35 retrograde, and in latitude 33″.75 south. The longitude and latitude of the center of Venus from the sun's center, answering to the several right ascensions and declinations observed, may be determined in the following manner.

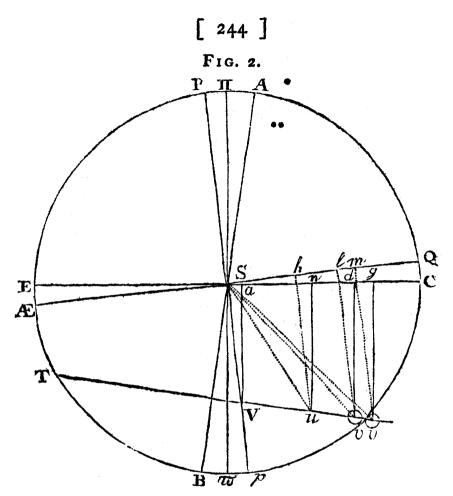


Fig. 2. Let the circle ΠE , ϖC represent the sun's disk; in which let E C be a portion of the ecliptic, $\Pi \varpi$ its axis, E Q a parallel to the equator, P p its axis, T V v the visible path of Venus on the sun, and AB the perpendicular to that path. The angle $QSC = PS\Pi =$ the inclination of the axis of the equator to the axis of the ecliptic, is given by calculations:

culation; then, at the internal contact, the fide S v, being the semidiameter of the sun, lessened by the femidiameter of Venus, is given, and also vl, the observed difference of declination; from whence may be found, by plain trigonometry, the angle vSI; from which, if the angle QSC be subtracted, there will remain the angle v S d; from whence, with S v, may be found Sa, the difference of longitude, and vd, the difference of latitude from the sun's center. in any other position, as at u, there will be given Sh, the difference of right ascension, and ub, the difference of declination; from whence may be found the angle u S b, and the fide S u: if from the angle uSb, the angle QSC be subtracted, there will remain the angle u S n; which, with the fide S u, before found, will give Sn, the difference of longitude, and un, the difference of latitude from the sun's center. At the conjunction in right ascension, SV is the observed difference of declination, and the compliment of the angle QSC is = the angle VSa; from whence will be found the difference of longitude Sa, and the difference of latitude Va, from the fun's center.

1. If a mean be taken of the 4th, 5th, 6th, and 7th of Mr. Hornsby's observations, and also of the times at 17^h 56′ 46″, the right ascension of the center of Venus will be 1″.2 before the sun's center, and the declination of it 10′ 10″.6; from whence the visible conjunction in right ascension was at 17^h 56′ 31″, and the visible declination south of the sun's center 10′ 10″.4: the visible longitude was, therefore, 1′ 5″.5 before the sun's center, and the visible latitude south of it 10′ 6″.9. From the computed

puted visible motion in longitude and latitude, by making the proper proportion, the visible ecliptic conjunction will be found at 17^h 40′ 3″ apparent time, at Shirburn, or at 17^h 44′ 4″ apparent time, at Greenwich, when the visible latitude was 9' 57".6 fouth of the sun's center. At 17h 56' 46", the parallax in longitude (supposing, as above, the horizontal parallax of the fun to be $10\frac{\pi}{3}$) will be 14", to be added to the visible longitude of Venus, to give her true longitude before the fun's center, and 20",5 to be subtracted from the visible latitude, to give the true latitude, as seen from the center of the earth. The true ecliptic conjunction, therefore, was 17h 36' 25" apparent time, at Sirburn, or 17h 40' 26" apparent time, at Greenwich, by making a proper proportion from the computed true motion of Venus from the fun; and the true latitude was then 9' 34.5" fouth.

2. From the mean of 10th, 11th, 12th, and 13th observations, at 19h 24' 9' apparent time, at Shirburn, the observed right ascension was 5' 40", and the observed declination was 11' 33.6"; from whence the visible longitude was 6' 52.2", and the visible latitude 10' 53".3, from the sun's center; and the visible ecliptic conjunction was at 17h 40' 23", at Shirburn, or at 17h 44' 24" apparent time, at Greenwich, with 9' 54.9" of visible latitude south. The parallax of longitude was 13.2", to be added to the visible longitude; and the parallax of latitude 18.1", to be subtracted from the visible latitude, to give the true latitude. The true ecliptic conjunction was, therefore, at 17h 36' 31", at Shirburn, or at

17^h 40' 32" apparent time, at Greenwich; the true latitude being then 9' 31".6 fouth.

3. From the mean of the 14th and 15th observations, at 19h 47' 29", the observed right ascension was 7' 6".3, and the observed declination 11' 57".6; from whence the visible longitude was 8' 20".5, and the visible latitude was 11' 8", from the sun's center; and the visible ecliptic conjunction was at 17h 41' 30", or at 17h 45' 31", apparent time, at Greenwich, with visible latitude 9' 57".2 south. The parallax of longitude was 12".5, to be added; and the parallax of latitude 17".4, to be subtracted, to give the true longitude and latitude. The true ecliptic conjunction was, therefore, at 17h 37' 42", at Shirburn, or at 17h 41' 43", apparent time, at Greenwich; the true latitude being then 9' 33".9 south.

4. At the internal contact, at Shirburn, at 20h 15' 10", if the motion in declination, answering to 3' of time, be added to the declination observed at the 16th observation, the declination of the center of Venus from the sun's center will be 12' 24".4; from whence the visible longitude was 10' 12".6, and the visible latitude 11' 23", from the sun's center; and the visible ecliptic conjunction was at 17h 40' 57', at Shirburn, or at 17h 44' 58', apparent time, at Greenwich, with 9' 56".2 of visible latitude south. The parallax of longitude, to be added, was 11".6; and the parallax of latitude 16".5, to be subtracted, to give the true longitude and latitude. The true ecliptic conjunction was, therefore, at 17h 37' 13", at Shirburn, or at 17h 41' 14", apparent time, at Greenwich; the true latitude being o' 33". I fouth.

5. The

5. The 2d observation made at Greenwich being dubious, if the mean of the 1st, 3d, 4th, and 5th, be taken at 19h 48' 39", apparent time, at Greenwich, the observed right ascension was 6' 52".4, and the observed declination 11' 52".4; from whence the visible longitude was 8' 6".1, and the visible latitude 11' 4".3, from the sun's center. The visible ecliptic conjunction was, therefore, 17h 46' 17", apparent time, at Greenwich, with 9' 55".5 of visible fouth latitude. The parallax of longitude, to be added, was 12".6; and the parallax of latitude, to be subtracted, 17".3, to give the true longitude and latitude from the sun's center. The true ecliptic conjunction, therefore, was at 17h 42' 28", apparent time, at Greenwich; when the true latitude was 9' 32".4.

I have omitted the computation of the longitude, latitude, and of the visible and true conjunction from the internal contact, at Greenwich, and the difference of declination, as given in my last letter; because there must have been some mistake in reading the numbers of the micrometer, or in setting them, or the times, down: for they differ too much from all the above, which correspond so well with each other, (though made at different places, and with different instruments) and give the true latitude, at the ecliptic conjunction, about 8" less, that we cannot safely de-

pend upon them.

If, therefore, we suppose the visible ecliptic conjunction to have happened at 17^h 45′ 3″, apparent time, at Greenwich, being the mean of the five foregoing deductions, where the greatest difference is no more than 2′ 13″ of time, or 8″ of visible longitude, with

with 9' 56".3 of visible south latitude, from the sun's center; where the greatest difference is no more than 2".7 in latitude, we cannot much err from the truth: and also, from the mean of the same deductions, the true ecliptic conjunction, as seen from the earth's center, will be at 17h 41' 17", with 9' 33".1 of fouth latitude. The middle of the transit was, therefore, at 17h 20' 5"; and the nearest approach of the centers 9' 26".8. The latitude then was 9' 20".6 fouth; but the longitude of Venus being augmented by the aberration of light 3"7, equivalent to 56" of time, by which the true ecliptic conjunction was accelerated, the true equated conjunction was at 17h 42' 13". The error in latitude, caused by the aberration of light, was 1".4, by which it was diminished; the equated latitude, therefore, was 9' 34".5.

The equation of time was then i' 52", to be subtracted from the apparent time, to give the mean; confequently, the true equated ecliptic conjunction. as feen from the earth's center, was at 17h 40' 21", mean time, at Greenwich. The true place of the fun, corrected by observation, was, at that time, 2° 15° 36′ 12"; and, consequently, the heliocentric place of Venus was 8s 15° 36' 12", with the geocentric latitude 9' 34".5. Now, in this case, the geocentric latitude is to the heliocentric latitude, as the distance of Venus from the sun is to the distance of Venus from the earth; and therefore, the planet's latitude, as feen from the fun, was 3' 48".5. If we fuppose the inclination of the orbit of Venus to be 3° 23' 20", as determined by Dr. Halley and M. Casfini, the distance of Venus from the node will be Vol. LII. 1° 4′ 20″:

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1° 4′ 20″; consequently, its true place 2° 14° 31′ 52″ on the day of the transit. The effect of refraction is not taken into these calculations; because, at the first observations, when its effect would have been greatest, it amounted only to a very small part of a second.

These, my Lord, are the Conclusions, which I have been able to deduce, from the observations made at your Lordship's own observatory, and at the Royal Observatory at Greenwich. They are as faithfully related, as they were scrupulously calculated; and if they meet with the approbation of your Lordship, and of the Royal Society, I shall think myself sufficiently rewarded, for the Labour of a long and tedious calculation.

I am,

With the greatest respect,

My Lord,

Your Lordship's,

and the Royal Society's,

much obliged,

and most obedient,

humble servant.

Oxford, Dec. 15, 1761,

Nathanael Bliss.